

# Assessing the impact of renewable energy sources on the electricity price level and variability - a Quantile Regression approach

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# Electricity markets

## Stylized facts

- the supply **MUST** meet the demand at every hour on every day
- limited storage possibilities
- changes of the production structure: from centrally planned generators into variable renewable units

# Increase of RES share in generation mix

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- the fall of marginal costs
- the uncertainty of generation
- difficulties of balancing the market

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Do RES impact electricity prices?

# Literature

- Merit-order effect: Ketterer (2014), Woo et al. (2011), Nihcolson et al. (2010), Gürtler, Paulsen (2018)
- Effect on variance:
  - Wind increases the volatility: Ketterer (2014), Cló et al. (2015), Rintamäki et al. (2017), Woo et al. (2011)
  - Solar reduces the volatility: Rintamäki et al. (2017), Paraschiv et al. (2014)
- Different models: ARX-GARCH (Ketterer, 2014), ARX (Woo et al., 2011 and Cló et al., 2015), realized volatility

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- Different models: ARX-GARCH (Ketterer, 2014), ARX (Woo et al., 2011 and Cló et al., 2015), realized volatility
- No formal comparison of strength of the effect for different RES

# Questions

- How do RES impact the level and variability of prices?
- Which RES: Solar or Wind have a stronger price-reduction effect?
- Do both RES increase or reduce the price variance?
- Does the effect of RES on the day-ahead prices depend on the level of demand/total load?

# Data

## Data

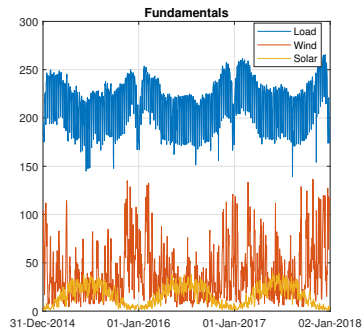
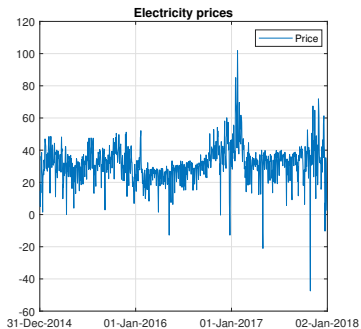
- Germany (EPEX)
- period: 01.01.2015-31.12.2017

The market is described by daily averages of:

- the day-ahead price,  $P_t$
- the forecast of load,  $L_t$
- the forecast of wind generation,  $W_t$
- the forecast of solar generation,  $S_t$



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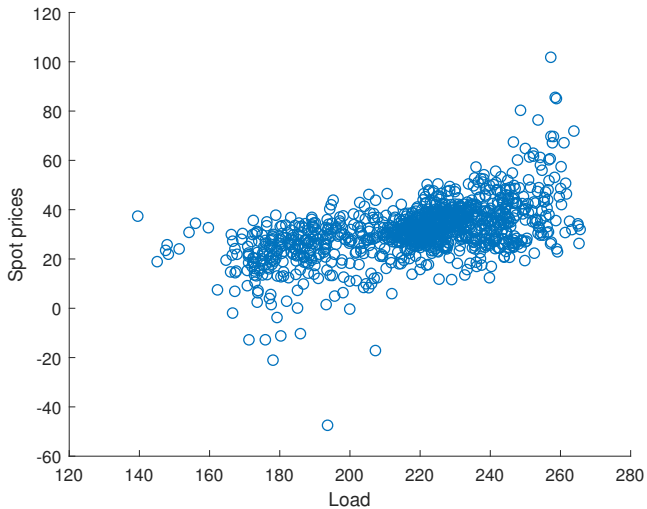
# Data statistics

**Table:** Statistical properties.

	Prices	Load	Wind	Solar
	Normality test (J-B)			
test	1838.8	58.21	258.0	75.68
p-value	< 0.01	< 0.01	< 0.01	< 0.01
	Non-stationarity (ADF)			
test	-6.992	-3.825	-7.723	-3.091
p-value	< 0.01	0.003	< 0.01	0.028

Note: the ADF test is based on a regression with seven lags and allows for a drift under the alternative.

# Data



# Quantile regression (QR) model - a linear effect

A linear model

$$P_t(\tau) = \alpha_{0,\tau} D_t + \beta_{\tau}^L L_t + \beta_{\tau}^S S_t + \beta_{\tau}^W W_t + \sum_{p=1}^7 \theta_{p,\tau} P_{t-p}, \quad (1)$$

where

- $P_t(\tau)$  is a  $\tau$  conditional quantile of the price  $P_t$
- $\beta_{\tau}^L$ ,  $\beta_{\tau}^S$  and  $\beta_{\tau}^W$  describe the influence of corresponding fundamentals:  $L_t$ ,  $S_t$  and  $W_t$  on  $P_t(\tau)$
- $\theta_{p,\tau}$  are the autoregressive parameters

# QR model - a non-linear effect

A non-linear model (2)

$$P_t(\tau) = \alpha_{0,\tau} D_t + \sum_{i=1}^3 \beta_{i,\tau}^L L_{i,t} + \sum_{i=1}^3 \beta_{i,\tau}^S S_{i,t} + \sum_{i=1}^3 \beta_{i,\tau}^W W_{i,t} + \sum_{p=1}^7 \theta_{p,\tau} P_{t-p}$$

where

- $L_{i,t} = I_i L_t$ ,  $S_{i,t} = I_i S_t$  and  $W_{i,t} = I_i W_t$ ,
- $I_1 = \mathbf{1}_{L_t < L(0.1)}$ ,  $I_2 = \mathbf{1}_{L(0.1) \leq L_t \leq L(0.9)}$  and  $I_3 = \mathbf{1}_{L_t > L(0.9)}$ , where  $L(\tau)$  describes the  $\tau$  unconditional quantile of  $L$

# Estimation of QR models

The estimator minimized the pinball loss function (Koenker and Bassett, 1978)

$$\min_{\psi_\tau \in \Psi} \sum_t \rho_\tau(P_t - X_t \psi_\tau),$$

where

$$\rho_\tau(P_t - X_t \psi_\tau) = \begin{cases} \tau(P_t - X_t \psi_\tau) & \text{when } P_t > X_t \psi_\tau \\ (\tau - 1)(P_t - X_t \psi_\tau) & \text{when } P_t \leq X_t \psi_\tau. \end{cases}$$

The variables

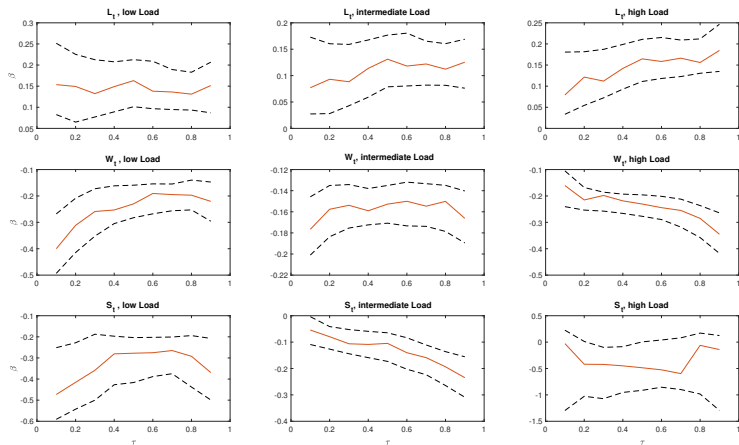
- $X_t = [D_t, L_t, S_t, W_t, P_{t-1}, \dots, P_{t-p}]$  for model (1)
- $X_t = [D_t, L_{1,t}, L_{2,t}, L_{3,t}, S_{1,t}, S_{2,t}, S_{3,t}, W_{1,t}, W_{2,t}, W_{3,t}, P_{t-1}, \dots, P_{t-p}]$  for model (2).

# Describing and testing the merit order effect

Merit order effect hypothesis:

- the influence of RES on prices is negative:  $\beta_{\tau}^S \leq 0$  and  $\beta_{\tau}^W \leq 0$   
or  $\beta_{i,\tau}^S \leq 0$  and  $\beta_{i,\tau}^W \leq 0$ ,
- an increase of Load ( $L_t$ ) leads to higher prices:  $\beta_{\tau}^L \geq 0$  or  
 $\beta_{i,\tau}^L \geq 0$
- the level of Load impact the merit-order effect

# Estimates of $\beta_{i,\tau}$ for different quantiles and Load levels





# The comparison of Wind and Solar effects

Which, Wind or Solar, has a stronger price dampening effect?

- both RES have  $\beta_{i,T}^W < 0$ ,  $\beta_{i,T}^S < 0$

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- p-values obtained by block bootstrap with block size equal 14, as in Fitzenberger (1998).

# The comparison of Wind and Solar effects

$\tau$	$\beta_{\tau}^W - \beta_{\tau}^S$	$\beta_{1,\tau}^W - \beta_{1,\tau}^S$	$\beta_{2,\tau}^W - \beta_{2,\tau}^S$	$\beta_{3,\tau}^W - \beta_{3,\tau}^S$
0.1	-0.111***	0.073	-0.122***	-0.132
0.2	-0.059***	0.104	-0.078***	0.204
0.3	-0.045**	0.100	-0.047***	0.225
0.4	-0.027	0.027	-0.050**	0.231
0.5	-0.029	0.048	-0.048	0.255
0.6	0.010	0.085	-0.010	0.281
0.7	0.027	0.070**	0.004	0.342
0.8	0.058**	0.095**	0.043	-0.224
0.9	0.083*	0.149**	0.068	-0.204

Note: the asterisks \*, \*\* and \*\*\* indicate rejection of null

$H_0 : \beta_{\tau}^W - \beta_{\tau}^S = 0$  at the significance levels 10%, 5% and 1%, respectively.

# Describing the impact on the variability

The variability is decied by the  $IQR_t = P_t(0.9) - P_t(0.1)$

$$IQR_t = \alpha_0 D_t + \sum_{i=1}^3 \beta_i^L L_{i,t} + \sum_{i=1}^3 \beta_i^S S_{i,t} + \sum_{i=1}^3 \beta_i^W W_{i,t} + \sum_{p=1}^7 \theta_p Y_{t-p},$$

where

- $\alpha_0 = \alpha_{0,0.9} - \alpha_{0,0.1}$
- $\beta_i^* = \beta_{i,0.9}^* - \beta_{i,0.1}^*$
- $\theta_p = \theta_{p,0.9} - \theta_{p,0.1}$

# Testing the impact on variability

The impact of fundamentals on  $IQR_t$  is described by  $\beta_i^*$

- when  $\beta_i^* > 0$  then an increase of the variable leads to a higher uncertainty,
- when  $\beta_i^* < 0$  then an increase of the variable leads to a fall of uncertainty,
- p-values obtained with block bootstrap

# The impact on the price volatility

Variable	Coefficient	Value
Load	$\beta^L$	0.0812
	$\beta_1^L$	-0.0021
	$\beta_2^L$	0.0483
	$\beta_3^L$	0.1053*
Wind	$\beta^W$	-0.0061
	$\beta_1^W$	0.1794**
	$\beta_2^W$	0.0104
	$\beta_3^W$	-0.1844***
Solar	$\beta^S$	-0.200***
	$\beta_1^S$	0.1037
	$\beta_2^S$	-0.1805***
	$\beta_3^S$	-0.1127



# Conclusions

- The merit-order effect is observable for all the fundamental variables
- The impact on the price level depends on the level of the load:
  - for the **median**, both RES have the same merit order effects
  - the effect of Wind is **stronger** than that of Solar for low quantiles of prices and the intermediate Load
  - the effect of Wind is **weaker** than that of Solar for high quantiles and the low Load

# Conclusions

The influence on price variability:

- Load **increases** the *IQR* when Load is high
- Wind **rises** the variability when Load is low and **reduces** it when Load is high
- Solar **reduces** the *IQR* for intermediate Load

# Conclusions

- The Quantile Regression approach offers an interesting alternative for estimating the changes of volatility:
  - a semi-parametric approach
  - is simpler to estimate than the ARX-GARCH model
  - is flexible when specifying the form of the conditional heteroscedasticity
  - standard errors could be obtained via simulation techniques (bootstrap)